



# SCAILD in abinit

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# Outline

1 Motivation

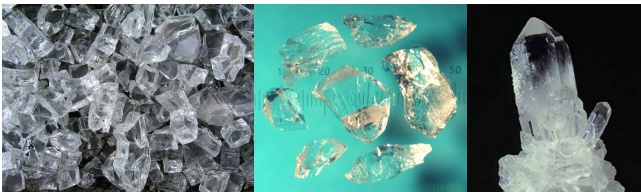
2 Formalism

3 Conclusions



# ab initio phase diagrams...

- How to determine the stablest phase at given conditions?
- Minimize appropriate (Gibbs) Free energy
- NVT ensemble:  $F=U-TS$
- NPT ensemble:  $Gibbs=F+pV$
- Works in principle for any phase transition (displacive)





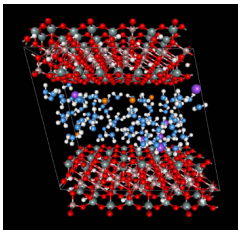
# Free Energies

- Thermodynamical stability  $\leftarrow$  lowest free energy
- Entropic effects can stabilize different phases for  $T > 0$
- Also need candidate dynamically stable phases
- Metastable states
  - enforced by symmetry or
  - “authentic”



# Standard methods I

- Do Molecular Dynamics trajectory, explore phase space
- *very* slow to get to ergodicity
- either spontaneously relaxes to correct phase
- or compare average energies





## Standard methods II

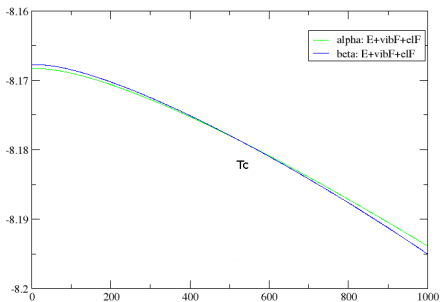
- 0K EOS - suppose  $U(V)$  independent of  $T$
- Vibrational entropy from phonons at  $T = 0$ ,  $V = V_0$
- Quasi-harmonic approximation - take  $V(T)$  into account
- Add  $e^-$  entropy (usu. negligible)
- Extrapolation of  $F(V,T)$  - fit polynomials in  $T$
- e.g. **Albe PRB 55 6203 (1997)**

$$F^{vib} = \frac{1}{N} \sum_i^{3N} \frac{\hbar\omega_i}{2} + k_B T \ln \left[ 1 - \exp\left(-\frac{\hbar\omega_i}{k_B T}\right) \right]$$



## Standard methods III

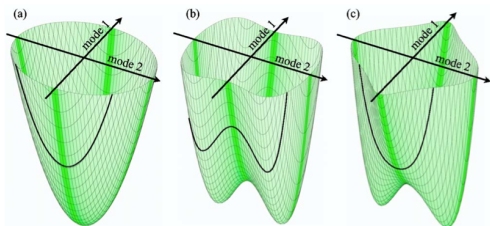
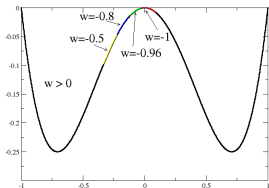
- Calculate  $U(V)$  and phonons for two phases
- Add  $F^{vib}(T)$ , and compare
- Thm expansion  $\rightarrow$  phonons at high-T volume
- impossible with unstable phonons





# Issues

- Physically  $\omega$  changes with T!
- Lack of symmetry constraints
- Finite T phonons explore anharmonicity (even 1 mode)
- Coupling of (an)harmonic phonons

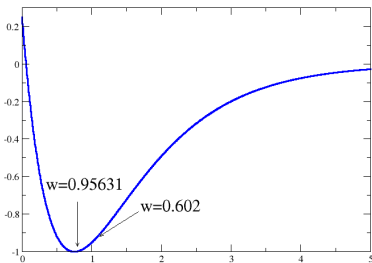






# Self-consistent phonons

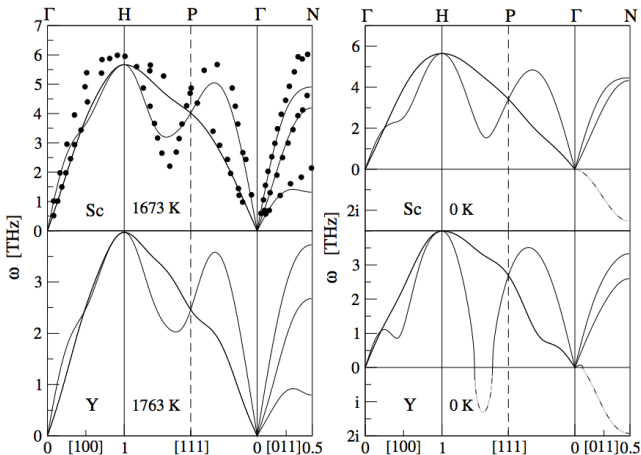
- Born-like method: Souvatzis et al. PRL 100 095901 (2008)
- Calculate phonons at  $T > 0$  “self-consistently”
- Phonon displacements are “thermalized”
- Takes anharmonicity into account





# Self-consistent phonons

- Example from Souvatzis CMS **44**, 888: high-T stability of BCC phases of Sc and Y





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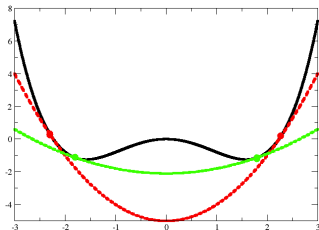
# Formalism I

Relate forces and phonon frequencies:

$$\vec{F}_R = - \sum_{R'} \Phi(R - R') U_{R'} \Rightarrow \vec{F}_q = - \sum_s M \omega_{qs}^2 \mathcal{A}_{qs} \vec{\epsilon}_{qs}$$

FT of real space  $\vec{F}$  wrt lattice vectors

beyond normal regime you pretend the well is harmonic...





## Formalism II

Cartesian vs. normal modes

$$U_R = \frac{1}{\sqrt{MN}} \sum_{qs} Q_{qs} \vec{\epsilon}_{qs} e^{iqR}$$

Normal modes are Boson-occupied  $T > 0$

$$\langle Q_{qs}^\dagger Q_{qs} \rangle = \frac{\hbar}{\omega_{qs}} \left[ \frac{1}{2} + n\left(\frac{\hbar\omega_{qs}}{k_B T}\right) \right]$$

$$A_{qs} = \pm \sqrt{\frac{\langle Q_{qs}^\dagger Q_{qs} \rangle}{M}}$$



## Formalism III

- Relate forces to phonon frequencies, through classical displacements

$$\omega_{qs} = \left[ -\frac{1}{M} \frac{\vec{\epsilon}_{qs} \cdot \vec{F}_q}{\mathcal{A}_{qs}} \right]^{1/2}$$

- renormalized frequencies (in principle to all orders!):

$$\bar{\omega}_{qs}^2 = \omega_{qs}^2 \left( 1 + \frac{\sqrt{M}}{2} \sum \Phi^3 \epsilon_{k_1 s_1} \epsilon_{k_2 s_2} \epsilon_{k_s} \frac{\mathcal{A}_{k_1 s_1} \mathcal{A}_{k_2 s_2}}{\mathcal{A}_{ks} \omega_{ks}^2} + \dots \right)$$



# Formalism IV

Cycle to “self-consistency”:

- $\omega \rightarrow$  normal mode displacements  $\mathcal{A}$
- $\mathcal{A} \rightarrow$  atom displacements  $\rightarrow \vec{F}$
- $\mathcal{A}$  and  $\vec{F} \rightarrow$  new  $\omega$



# Hypotheses

- Hyp 1: phonon polarization vectors unchanged
- Hyp 2: no phonon lifetime effects
- Hyp 3: no thermal expansion





# In practice

- 1 Get T=0 phonons
- 2 Use a supercell, move atoms along normal modes
- 3 → displacements for given T
- 4 DFT forces → effective frequencies
- 5 → new free energy and normal modes
- 6 symmetrize  $\omega$
- 7 get configuration averaged  $\omega$



# Tricks

- 1 Running average of frequencies  $\rightarrow$  config. avg.
- 2 Interpolation of  $\bar{\omega}_{qs} \rightarrow$  better  $F(T)$
- 3 Choice of amplitude for displacement:  $\pm 1$  (could be Gaussian)
- 4 Populate negative modes as though they were positive



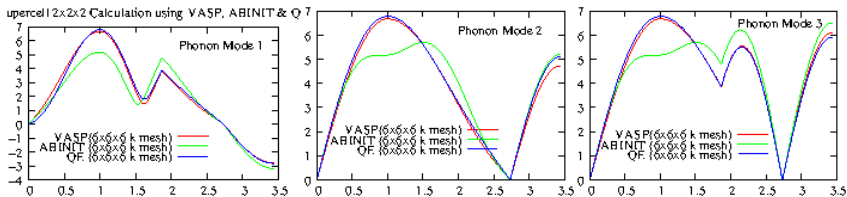
# Limitations

- 1 Method inherently requires large supercells (4x4x4 usually not converged)
- 2 no direct access to 3rd or 4th order derivatives or other info
- 3 no evolution of cell or  $\epsilon$
- 4 dielectric effects in supercell (Parlinskii) are gross



# scphon adaptation

- Original VASP scripts adapted to Abinit and Qespresso by Srijan Kumar Saha
- parse abinit output for forces and feed in correct atomic positions and supercell
- remaining difference due to psp (Ti without SC states)





# Abinit workflow

- 1 Run normal DFPT for  $q=2 \times 2 \times 2$  MP
- 2 `anaddb` with "outscphon 1" to get:
- 3 `xx_PCINFO`, `xx_PHFRQ`, `xx_PHVEC` copied to abinit run
- 4 Supercell equivalent to phonon  $q$ -grid
- 5 Implemented in ABINIT as MD, but excluded from Guillermo's library (77\_ddb dependencies)

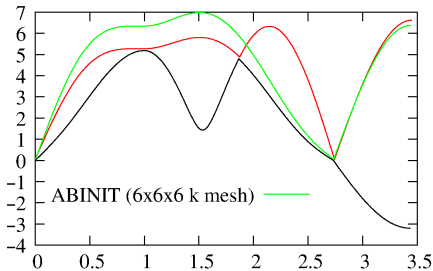
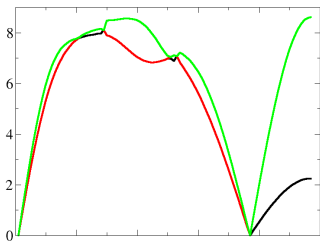
## variables

<code>ionmov 30</code>	<code>nsym 1</code>	<code>acell *= 2</code>
<code>scphon_temp 300 K</code>	<code>scphon_supercell</code>	<code>2 2 2</code>



# Ye goode aulde code

- Still testing after all these years
- Low T limit incorrect, bug left somewhere
- 2x2x2 supercell of Ti
- order of magnitude fine, but some tricks missing
- scphon\_XX subroutines





# Ye goode aulde code

- Phonons appear to be stabilized very systematically (too much?)
- Phase stability from free energy differences
- 
- test v6 number 100, uses output for AI from v6 tests 85-88



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## Conclusions

- Heavier than standard phonon calculations of  $F(T)$
- Still easier than coding full anharmonic effects...
- Not clear if it has precision for good  $T_c$  estimation



## Perspectives

- Try on ferroelectrics or geological phases
- Abinit version should have better dipole-dipole term
- lifetimes related to variance of  $\bar{\omega}$ ?



# Discussions

## Ideas

- Petros Souvatzis (Uppsala)
- Karsten Albe (Dresden)
- Olle Ericsson (Uppsala)